## **NAG Library Routine Document**

## F06SLF (ZTPSV)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

#### 1 Purpose

F06SLF (ZTPSV) solves a complex triangular system of equations, stored in packed form, with a single right hand side.

#### 2 Specification

```
SUBROUTINE F06SLF (UPLO, TRANS, DIAG, N, AP, X, INCX)
INTEGER
COMPLEX (KIND=nag_wp) AP(*), X(*)
CHARACTER(1) UPLO, TRANS, DIAG
```

The routine may be called by its BLAS name ztpsv.

### 3 Description

F06SLF (ZTPSV) performs one of the matrix-vector operations

$$x \leftarrow A^{-1}x, \quad x \leftarrow A^{-\mathsf{T}}x \quad \text{ or } \quad x \leftarrow A^{-\mathsf{H}}x,$$

where A is an n by n complex triangular matrix, stored in packed form, and x is an n-element complex vector.  $A^{-T}$  denotes  $(A^T)^{-1}$  or equivalently  $(A^{-1})^T$ ;  $A^{-H}$  denotes  $(A^H)^{-1}$  or equivalently  $(A^{-1})^H$ .

No test for singularity or near-singularity of A is included in this routine. Such tests must be performed before calling this routine.

#### 4 References

None.

#### 5 Parameters

Input

On entry: specifies whether A is upper or lower triangular.

UPLO = 'U'

A is upper triangular.

UPLO = 'L'

A is lower triangular.

Constraint: UPLO = 'U' or 'L'.

Input

On entry: specifies the operation to be performed.

$$\begin{aligned} \text{TRANS} &= \text{'N'} \\ x \leftarrow A^{-1}x. \end{aligned}$$

$$\begin{aligned} \mathsf{TRANS} &= \mathsf{'T'} \\ x \leftarrow A^{-\mathsf{T}} x. \end{aligned}$$

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$$TRANS = 'C'$$
$$x \leftarrow A^{-H}x.$$

Constraint: TRANS = 'N', 'T' or 'C'.

#### 3: DIAG - CHARACTER(1)

Input

On entry: specifies whether A has nonunit or unit diagonal elements.

DIAG = 'N'

The diagonal elements are stored explicitly.

DIAG = 'U'

The diagonal elements are assumed to be 1, and are not referenced.

Constraint: DIAG = 'N' or 'U'.

#### 4: N – INTEGER

Input

On entry: n, the order of the matrix A.

Constraint:  $N \ge 0$ .

#### 5: AP(\*) - COMPLEX (KIND=nag\_wp) array

Input

**Note**: the dimension of the array AP must be at least  $N \times (N+1)/2$ .

On entry: the n by n triangular matrix A, packed by columns.

More precisely,

if UPLO = 'U', the upper triangle of A must be stored with element  $A_{ij}$  in AP(i+j(j-1)/2) for  $i \leq j$ ;

if UPLO = 'L', the lower triangle of A must be stored with element  $A_{ij}$  in AP(i + (2n - j)(j - 1)/2) for  $i \ge j$ .

If DIAG = 'U', the diagonal elements of A are assumed to be 1, and are not referenced; the same storage scheme is used whether DIAG = 'N' or 'U'.

#### 6: X(\*) – COMPLEX (KIND=nag wp) array

Input/Output

**Note**: the dimension of the array X must be at least  $max(1, 1 + (N - 1) \times |INCX|)$ .

On entry: the vector x.

If INCX > 0,  $x_i$  must be stored in  $X(1 + (i-1) \times INCX)$ , for i = 1, 2, ..., N.

If INCX < 0,  $x_i$  must be stored in  $X(1-(N-i) \times INCX)$ , for i = 1, 2, ..., N.

On exit: the updated vector x stored in the array elements used to supply the original vector x.

#### 7: INCX – INTEGER

Input

On entry: the increment in the subscripts of X between successive elements of x.

Constraint: INCX  $\neq 0$ .

#### 6 Error Indicators and Warnings

None.

### 7 Accuracy

Not applicable.

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## 8 Parallelism and Performance

Not applicable.

## **9** Further Comments

None.

# 10 Example

None.

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