Input

NAG Library Routine Document F08ACF (DGEMORT)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

F08ACF (DGEMQRT) multiplies an arbitrary real matrix C by the real orthogonal matrix Q from a QR factorization computed by F08ABF (DGEORT).

2 Specification

```
SUBROUTINE FO8ACF (SIDE, TRANS, M, N, K, NB, V, LDV, T, LDT, C, LDC, WORK, INFO)

INTEGER M, N, K, NB, LDV, LDT, LDC, INFO
REAL (KIND=nag_wp) V(LDV,*), T(LDT,*), C(LDC,*), WORK(*)
CHARACTER(1) SIDE, TRANS
```

The routine may be called by its LAPACK name dgemqrt.

3 Description

F08ACF (DGEMQRT) is intended to be used after a call to F08ABF (DGEQRT) which performs a QR factorization of a real matrix A. The orthogonal matrix Q is represented as a product of elementary reflectors.

This routine may be used to form one of the matrix products

$$QC, Q^{\mathsf{T}}C, CQ \text{ or } CQ^{\mathsf{T}},$$

overwriting the result on C (which may be any real rectangular matrix).

A common application of this routine is in solving linear least squares problems, as described in the F08 Chapter Introduction and illustrated in Section 10 in F08ABF (DGEQRT).

4 References

Golub G H and Van Loan C F (2012) *Matrix Computations* (4th Edition) Johns Hopkins University Press, Baltimore

5 Parameters

1: SIDE - CHARACTER(1)

On entry: indicates how Q or Q^{T} is to be applied to C.

SIDE = 'L'

SIDE — 'D'

Q or Q^{T} is applied to C from the right.

Q or Q^{T} is applied to C from the left.

Constraint: SIDE = 'L' or 'R'.

Mark 25 F08ACF.1

NAG Library Manual

2: TRANS - CHARACTER(1)

Input

On entry: indicates whether Q or Q^{T} is to be applied to C.

TRANS = 'N'

Q is applied to C.

TRANS = 'T'

 Q^{T} is applied to C.

Constraint: TRANS = 'N' or 'T'.

3: M – INTEGER

Input

On entry: m, the number of rows of the matrix C.

 $\textit{Constraint} \colon M \geq 0.$

4: N – INTEGER

Input

On entry: n, the number of columns of the matrix C.

Constraint: N > 0.

5: K – INTEGER

Input

On entry: k, the number of elementary reflectors whose product defines the matrix Q. Usually $K = \min(m_A, n_A)$ where m_A , n_A are the dimensions of the matrix A supplied in a previous call to F08ABF (DGEQRT).

Constraints:

if SIDE = 'L',
$$M \ge K \ge 0$$
; if SIDE = 'R', $N \ge K \ge 0$.

6: NB – INTEGER

Input

On entry: the block size used in the QR factorization performed in a previous call to F08ABF (DGEQRT); this value must remain unchanged from that call.

Constraints:

$$NB \ge 1$$
; if $K > 0$, $NB \le K$.

7: V(LDV,*) - REAL (KIND=nag_wp) array

Input

Note: the second dimension of the array V must be at least max(1, K).

On entry: details of the vectors which define the elementary reflectors, as returned by F08ABF (DGEQRT) in the first k columns of its array parameter A.

8: LDV – INTEGER

Input

On entry: the first dimension of the array V as declared in the (sub)program from which F08ACF (DGEMQRT) is called.

Constraints:

if SIDE = 'L', LDV
$$\geq \max(1, M)$$
; if SIDE = 'R', LDV $\geq \max(1, N)$.

9: T(LDT, *) - REAL (KIND=nag_wp) array

Input

Note: the second dimension of the array T must be at least max(1, K).

On entry: further details of the orthogonal matrix Q as returned by F08ABF (DGEQRT). The number of blocks is $b = \left\lceil \frac{k}{\text{NB}} \right\rceil$, where $k = \min(m, n)$ and each block is of order NB except for the

F08ACF.2 Mark 25

last block, which is of order $k - (b - 1) \times NB$. For the b blocks the upper triangular block reflector factors T_1, T_2, \ldots, T_b are stored in the NB by n matrix T as $T = [T_1 | T_2 | \ldots | T_b]$.

10: LDT – INTEGER Input

On entry: the first dimension of the array T as declared in the (sub)program from which F08ACF (DGEMQRT) is called.

Constraint: LDT \geq NB.

11: C(LDC, *) - REAL (KIND=nag wp) array

Input/Output

Note: the second dimension of the array C must be at least max(1, N).

On entry: the m by n matrix C.

On exit: C is overwritten by QC or Q^TC or CQ or CQ^T as specified by SIDE and TRANS.

12: LDC – INTEGER Input

On entry: the first dimension of the array C as declared in the (sub)program from which F08ACF (DGEMQRT) is called.

Constraint: LDC $\geq \max(1, M)$.

13: WORK(*) - REAL (KIND=nag_wp) array

Workspace

Note: the dimension of the array WORK must be at least $N \times NB$ if SIDE = L' and at least $M \times NB$ if SIDE = R'.

14: INFO – INTEGER Output

On exit: INFO = 0 unless the routine detects an error (see Section 6).

6 Error Indicators and Warnings

INFO < 0

If INFO = -i, argument i had an illegal value. An explanatory message is output, and execution of the program is terminated.

7 Accuracy

The computed result differs from the exact result by a matrix E such that

$$||E||_2 = O(\epsilon)||C||_2$$

where ϵ is the *machine precision*.

8 Parallelism and Performance

F08ACF (DGEMQRT) is not threaded by NAG in any implementation.

F08ACF (DGEMQRT) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this routine. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

Mark 25 F08ACF.3

F08ACF NAG Library Manual

9 Further Comments

The total number of floating-point operations is approximately 2nk(2m-k) if SIDE = 'L' and 2mk(2n-k) if SIDE = 'R'.

The complex analogue of this routine is F08AQF (ZGEMQRT).

10 Example

See Section 10 in F08ABF (DGEQRT).

F08ACF.4 (last) Mark 25