1 Purpose
Given a set of \( m \) features and a scoring mechanism for any subset of those features, \( \text{nag}_\text{best}_\text{subset}_\text{given}_\text{size}_\text{revcomm} \)(h05aac) selects the best \( n \) subsets of size \( p \) using a reverse communication branch and bound algorithm.

2 Specification

```c
#include <nag.h>
#include <nagh.h>

void nag_best_subset_given_size_revcomm (Integer *irevcm, Integer mincr,
    Integer m, Integer ip, Integer nbest, Integer *drop, Integer *lz,
    Integer z[], Integer *la, Integer a[], double bscore[], Integer bz[],
    Integer mincnt, double gamma, const double acc[], Integer icomm[],
    Integer licomm, double rcomm[], Integer lrcomm, NagError *fail)
```

3 Description
Given \( \Omega = \{x_i : i \in \mathbb{Z}, 1 \leq i \leq m\} \), a set of \( m \) unique features and a scoring mechanism \( f(S) \) defined for all \( S \subseteq \Omega \) then \( \text{nag}_\text{best}_\text{subset}_\text{given}_\text{size}_\text{revcomm} \)(h05aac) is designed to find \( S_{o1} \subseteq \Omega, |S_{o1}| = p \), an optimal subset of size \( p \). Here \( |S_{o1}| \) denotes the cardinality of \( S_{o1} \), the number of elements in the set.

The definition of the optimal subset depends on the properties of the scoring mechanism, if

\[
f(S_i) \leq f(S_j), \quad \text{for all } S_i \subseteq \Omega \text{ and } S_i \subseteq S_j\]

then the optimal subset is defined as one of the solutions to

\[
\max_{S \subseteq \Omega} f(S) \quad \text{subject to } |S| = p
\]

else if

\[
f(S_i) \geq f(S_j), \quad \text{for all } S_i \subseteq \Omega \text{ and } S_i \subseteq S_j\]

then the optimal subset is defined as one of the solutions to

\[
\min_{S \subseteq \Omega} f(S) \quad \text{subject to } |S| = p.
\]

If neither of these properties hold then \( \text{nag}_\text{best}_\text{subset}_\text{given}_\text{size}_\text{revcomm} \)(h05aac) cannot be used.

As well as returning the optimal subset, \( S_{o1} \), \( \text{nag}_\text{best}_\text{subset}_\text{given}_\text{size}_\text{revcomm} \)(h05aac) can return the best \( n \) solutions of size \( p \). If \( S_{oi} \) denotes the \( i \)th best subset, for \( i = 1, 2, \ldots, n - 1 \), then the \( (i + 1) \)th best subset is defined as the solution to either

\[
\max_{S \subseteq \Omega - \{S_{oi} : j \in \mathbb{Z}, 1 \leq j \leq i\}} f(S) \quad \text{subject to } |S| = p
\]

or

\[
\min_{S \subseteq \Omega - \{S_{oi} : j \in \mathbb{Z}, 1 \leq j \leq i\}} f(S) \quad \text{subject to } |S| = p
\]

depending on the properties of \( f \).

The solutions are found using a branch and bound method, where each node of the tree is a subset of \( \Omega \). Assuming that (1) holds then a particular node, defined by subset \( S_i \), can be trimmed from the tree if
f(S_i) < \hat{f}(S_{on})$ where $\hat{f}(S_{on})$ is the $n$th highest score we have observed so far for a subset of size $p$, i.e., our current best guess of the score for the $n$th best subset. In addition, because of (1) we can also drop all nodes defined by any subset $S_j$ where $S_j \subseteq S_i$, thus avoiding the need to enumerate the whole tree. Similar short cuts can be taken if (2) holds. A full description of this branch and bound algorithm can be found in Ridout (1988).

Rather than calculate the score at a given node of the tree nag_best_subset_given_size_revcomm (h05aac) utilizes the fast branch and bound algorithm of Somol et al. (2004), and attempts to estimate the score where possible. For each feature, $x_i$, two values are stored, a count $c_i$ and $\mu_i$, an estimate of the contribution of that feature. An initial value of zero is used for both $c_i$ and $\mu_i$. At any stage of the algorithm where both $f(S)$ and $f(S - \{x_i\})$ have been calculated (as opposed to estimated), the estimated contribution of the feature $x_i$ is updated to

$$c_i \mu_i + \left[ f(S) - f(S - \{x_j\}) \right] \over c_i + 1$$

and $c_i$ is incremented by 1, therefore at each stage $\mu_i$ is the mean contribution of $x_i$ observed so far and $c_i$ is the number of observations used to calculate that mean.

As long as $c_i \geq k$, for the user-supplied constant $k$, then rather than calculating $f(S - \{x_i\})$ this function estimates it using $\hat{f}(S - \{x_i\}) = f(S) - \gamma \mu_i$ or $\hat{f}(S) - \gamma \mu_i$ if $f(S)$ has been estimated, where $\gamma$ is a user-supplied scaling factor. An estimated score is never used to trim a node or returned as the optimal score.

Setting $k = 0$ in this function will cause the algorithm to always calculate the scores, returning to the branch and bound algorithm of Ridout (1988). In most cases it is preferable to use the fast branch and bound algorithm, by setting $k > 0$, unless the score function is iterative in nature, i.e., $f(S)$ must have been calculated before $f(S - \{x_i\})$ can be calculated.

4 References

5 Arguments
Note: this function uses reverse communication. Its use involves an initial entry, intermediate exits and re-entries, and a final exit, as indicated by the argument irevcm. Between intermediate entries and re-entries, all arguments other than bscore must remain unchanged.

1:   irevcm – Integer * 

       Input/Output

       On initial entry: must be set to 0.

       On intermediate exit: irevcm = 1 and before re-entry the scores associated with la subsets must be calculated and returned in bscore.

       The la subsets are constructed as follows:

       drop = 1

       The jth subset is constructed by dropping the features specified in the first lz elements of z and the single feature given in a[j - 1] from the full set of features, Ω. The subset will therefore contain m - lz - 1 features.

       drop = 0

       The jth subset is constructed by adding the features specified in the first lz elements of z and the single feature specified in a[j - 1] to the empty set, θ. The subset will therefore contain lz + 1 features.
In both cases the individual features are referenced by the integers 1 to \( m \) with 1 indicating the first feature, 2 the second, etc., for some arbitrary ordering of the features. The same ordering must be used in all calls to nag_best_subset_given_size_revcomm (h05aac).

If \( l_a = 0 \), the score for a single subset should be returned. This subset is constructed by adding or removing only those features specified in the first \( l_z \) elements of \( z \).

If \( l_z = 0 \), this subset will either be \( \emptyset \) or \( \Omega \).

The score associated with the \( j \)th subset must be returned in \( b_{score}\[j - 1\] \).

On intermediate re-entry: \( irevcm \) must remain unchanged.

On final exit: \( irevcm = 0 \), and the algorithm has terminated.

Constraint: \( irevcm = 0 \) or 1.

2: \( mincr \) – Integer

\( mincr = 1 \) \( f(S_i) \leq f(S_j) \), i.e., the subsets with the largest score will be selected.

\( mincr = 0 \) \( f(S_i) \geq f(S_j) \), i.e., the subsets with the smallest score will be selected.

For all \( S_j \subseteq \Omega \) and \( S_i \subseteq S_j \).

Constraint: \( mincr = 0 \) or 1.

3: \( m \) – Integer

\( m \), the number of features in the full feature set.

Constraint: \( m \geq 2 \).

4: \( ip \) – Integer

\( p \), the number of features in the subset of interest.

Constraint: \( 1 \leq ip \leq m \).

5: \( nbest \) – Integer

\( n \), the maximum number of best subsets required. The actual number of subsets returned is given by \( l_a \) on final exit. If on final exit \( l_a \neq nbest \) then \( fail\_code = \text{NE_TOO_MANY} \) is returned.

Constraint: \( nbest \geq 1 \).

6: \( drop \) – Integer *

\( drop \) need not be set.

On intermediate exit: flag indicating whether the intermediate subsets should be constructed by dropping features from the full set (\( drop = 1 \)) or adding features to the empty set (\( drop = 0 \)). See \( irevcm \) for details.

On intermediate re-entry: \( drop \) must remain unchanged.

On final exit: \( drop \) is undefined.

7: \( l_z \) – Integer *

\( l_z \) need not be set.

On intermediate exit: the number of features stored in \( z \).

On intermediate re-entry: \( l_z \) must remain unchanged.
On final exit: \(lz\) is undefined.

8: \(z[m - ip]\) – Integer  
   \[Input/Output\]
   
   On initial entry: \(z\) need not be set.
   
   On intermediate exit: \(z[i - 1]\), for \(i = 1, 2, \ldots, lz\), contains the list of features which, along with those specified in \(a\), define the subsets whose score is required. See irevcm for additional details.
   
   On intermediate re-entry: \(z\) must remain unchanged.
   
   On final exit: \(z\) is undefined.

9: \(la\) – Integer *  
   \[Input/Output\]
   
   On initial entry: \(la\) need not be set.
   
   On intermediate exit: if \(la > 0\), the number of subsets for which a score must be returned.
   
   If \(la = 0\), the score for a single subset should be returned. See irevcm for additional details.
   
   On intermediate re-entry: \(la\) must remain unchanged.
   
   On final exit: the number of best subsets returned.

10: \(a[max(nbest, m)]\) – Integer  
   \[Input/Output\]
   
   On initial entry: \(a\) need not be set.
   
   On intermediate exit: \(a[j - 1]\), for \(j = 1, 2, \ldots, la\), contains the list of features which, along with those specified in \(z\), define the subsets whose score is required. See irevcm for additional details.
   
   On intermediate re-entry: \(a\) must remain unchanged.
   
   On final exit: \(a\) is undefined.

11: \(bscore[max(nbest, m)]\) – double  
   \[Input/Output\]
   
   On initial entry: \(bscore\) need not be set.
   
   On intermediate exit: \(bscore\) is undefined.
   
   On intermediate re-entry: \(bscore[j - 1]\) must hold the score for the \(j\)th subset as described in irevcm.
   
   On final exit: holds the score for the \(la\) best subsets returned in \(bz\).

12: \(bz[m - ip] \times nbest\) – Integer  
   \[Input/Output\]
   
   Note: where \(BZ(i, j)\) appears in this document, it refers to the array element \(bz((j - 1) \times (m - ip) + i - 1)\).
   
   On initial entry: \(bz\) need not be set.
   
   On intermediate exit: \(bz\) is used for storage between calls to nag_best_subset_given_size_revcomm (h05aac).
   
   On intermediate re-entry: \(bz\) must remain unchanged.
   
   On final exit: the \(j\)th best subset is constructed by dropping the features specified in \(BZ(i, j)\), for \(i = 1, 2, \ldots, m - ip\) and \(j = 1, 2, \ldots, la\), from the set of all features, \(\varnothing\). The score for the \(j\)th best subset is given in \(bscore[j - 1]\).

13: \(\text{mincnt}\) – Integer  
   \[Input\]
   
   On entry: \(k\), the minimum number of times the effect of each feature, \(x_i\), must have been observed before \(f(S - \{x_i\})\) is estimated from \(f(S)\) as opposed to being calculated directly.
   
   If \(k = 0\) then \(f(S - \{x_i\})\) is never estimated. If \(\text{mincnt} < 0\) then \(k\) is set to 1.
14: \( \text{gamma} \) – double

\( \text{Input} \)

\( \text{On entry:} \) \( \gamma \), the scaling factor used when estimating scores. If \( \text{gamma} < 0 \) then \( \gamma = 1 \) is used.

15: \( \text{acc}[2] \) – const double

\( \text{Input} \)

\( \text{On entry:} \) a measure of the accuracy of the scoring function, \( f \). Letting \( a_i = \epsilon_1 |f(S_i)| + \epsilon_2 \), then when confirming whether the scoring function is strictly increasing or decreasing (as described in \textit{minor}), or when assessing whether a node defined by subset \( S_i \) can be trimmed, then any values in the range \( f(S_i) \pm a_i \) are treated as being numerically equivalent.

If \( 0 \leq \text{acc}[0] \leq 1 \) then \( \epsilon_1 = \text{acc}[0] \), otherwise \( \epsilon_1 = 0 \).

If \( \text{acc}[1] \geq 0 \) then \( \epsilon_2 = \text{acc}[1] \), otherwise \( \epsilon_2 = 0 \).

In most situations setting both \( \epsilon_1 \) and \( \epsilon_2 \) to zero should be sufficient. Using a nonzero value, when one is not required, can significantly increase the number of subsets that need to be evaluated.

16: \( \text{icomm} | \text{licomm} \) – Integer

\( \text{Communication Array} \)

\( \text{On initial entry:} \ \text{icomm} \text{ need not be set.} \)

\( \text{On intermediate exit:} \ \text{icomm} \text{ is used for storage between calls to nag_best_subset_given_size_revcomm (h05aac).} \)

\( \text{On intermediate re-entry:} \ \text{icomm} \text{ must remain unchanged.} \)

\( \text{On final exit:} \ \text{icomm} \text{ is not defined. The first two elements, icomm}[0] \text{ and icomm}[1] \text{ contain the minimum required value for licomm and lrcomm respectively.} \)

17: \( \text{licomm} \) – Integer

\( \text{Input} \)

\( \text{On entry:} \) the length of the array \( \text{icomm} \). If \( \text{licomm} \) is too small and \( \text{licomm} \geq 2 \) then \textbf{fail.code} = \text{NE_ARRAY_SIZE} is returned and the minimum value for \( \text{licomm} \) and \( \text{lrcomm} \) are given by \( \text{icomm}[0] \) and \( \text{icomm}[1] \) respectively.

\textbf{Constraints:}

\[ \begin{align*}
\text{if } \text{mincnt} &= 0 \\
\text{licomm} &\geq 2 \times \max(\text{nbest}, \text{m}) + \text{m}(\text{m} + 2) + (\text{m} + 1) \times \max(\text{m} - \text{ip}, 1) + 27; \\
\text{otherwise } \text{licomm} &\geq 2 \times \max(\text{nbest}, \text{m}) + \text{m}(\text{m} + 3) + (2\text{m} + 1) \times \max(\text{m} - \text{ip}, 1) + 25.
\end{align*} \]

18: \( \text{rcomm} | \text{lrcomm} \) – double

\( \text{Communication Array} \)

\( \text{On initial entry:} \ \text{rcomm} \text{ need not be set.} \)

\( \text{On intermediate exit:} \ \text{rcomm} \text{ is used for storage between calls to nag_best_subset_given_size_revcomm (h05aac).} \)

\( \text{On intermediate re-entry:} \ \text{rcomm} \text{ must remain unchanged.} \)

\( \text{On final exit:} \ \text{rcomm} \text{ is not defined.} \)

19: \( \text{lrcomm} \) – Integer

\( \text{Input} \)

\( \text{On entry:} \) the length of the array \( \text{rcomm} \). If \( \text{lrcomm} \) is too small and \( \text{lrcomm} \geq 2 \) then \textbf{fail.code} = \text{NE_ARRAY_SIZE} is returned and the minimum value for \( \text{licomm} \) and \( \text{lrcomm} \) are given by \( \text{icomm}[0] \) and \( \text{icomm}[1] \) respectively.

\textbf{Constraints:}

\[ \begin{align*}
\text{if } \text{mincnt} &= 0, \text{lrcomm} \geq 9 + \text{nbest} + \text{m} \times \max(\text{m} - \text{ip}, 1); \\
\text{otherwise } \text{lrcomm} &\geq 8 + \text{m} + \text{nbest} + \text{m} \times \max(\text{m} - \text{ip}, 1).
\end{align*} \]

20: \( \text{fail} \) – \textbf{NagError} *

\( \text{Input/Output} \)

The NAG error argument (see Section 3.6 in the Essential Introduction).
6 Error Indicators and Warnings

**NE_ALLOC_FAIL**
Dynamic memory allocation failed.
See Section 3.2.1.2 in the Essential Introduction for further information.

**NE_ARRAY_SIZE**
On entry, \( \text{licomm} = (\text{value}), \ \text{lcomm} = (\text{value}) \).
Constraint: \( \text{licomm} \geq (\text{value}), \ \text{lcomm} \geq (\text{value}) \).
The minimum required values for \( \text{licomm} \) and \( \text{lcomm} \) are returned in \( \text{icomm}[0] \) and \( \text{icomm}[1] \) respectively.

**NE_BAD_PARAM**
On entry, argument \( (\text{value}) \) had an illegal value.

**NE_ILLEGAL_COMM**
\( \text{icomm} \) has been corrupted between calls.
\( \text{rcomm} \) has been corrupted between calls.

**NE_INT**
On entry, \( \text{irevcm} = (\text{value}) \).
Constraint: \( \text{irevcm} = 0 \) or \( 1 \).
On entry, \( \text{m} = (\text{value}) \).
Constraint: \( \text{m} \geq 2 \).
On entry, \( \text{mincr} = (\text{value}) \).
Constraint: \( \text{mincr} = 0 \) or \( 1 \).
On entry, \( \text{nbest} = (\text{value}) \).
Constraint: \( \text{nbest} \geq 1 \).

**NE_INT_2**
On entry, \( \text{ip} = (\text{value}) \) and \( \text{m} = (\text{value}) \).
Constraint: \( 1 \leq \text{ip} \leq \text{m} \).

**NE_INT_CHANGED**
\( \text{drop} \) has changed between calls.
On intermediate entry, \( \text{drop} = (\text{value}) \).
On initial entry, \( \text{drop} = (\text{value}) \).
\( \text{ip} \) has changed between calls.
On intermediate entry, \( \text{ip} = (\text{value}) \).
On initial entry, \( \text{ip} = (\text{value}) \).
\( \text{la} \) has changed between calls.
On entry, \( \text{la} = (\text{value}) \).
On previous exit, \( \text{la} = (\text{value}) \).
\( \text{lz} \) has changed between calls.
On entry, \( \text{lz} = (\text{value}) \).
On previous exit, \( \text{lz} = (\text{value}) \).
\( \text{m} \) has changed between calls.
On intermediate entry, \( \text{m} = (\text{value}) \).
On initial entry, \( \text{m} = (\text{value}) \).
\textbf{mincnt} has changed between calls.
On intermediate entry, \texttt{mincnt} = \langle value\rangle.
On initial entry, \texttt{mincnt} = \langle value\rangle.

\textbf{mincr} has changed between calls.
On intermediate entry, \texttt{mincr} = \langle value\rangle.
On initial entry, \texttt{mincr} = \langle value\rangle.

\textbf{nbest} has changed between calls.
On intermediate entry, \texttt{nbest} = \langle value\rangle.
On initial entry, \texttt{nbest} = \langle value\rangle.

\textbf{NE\_INTERNAL\_ERROR}
An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.
An unexpected error has been triggered by this function. Please contact NAG.
See Section 3.6.6 in the Essential Introduction for further information.

\textbf{NE\_NO\_LICENCE}
Your licence key may have expired or may not have been installed correctly.
See Section 3.6.5 in the Essential Introduction for further information.

\textbf{NE\_REAL}
\texttt{bscore}\[\langle value\rangle\] = \langle value\rangle, which is inconsistent with the score for the parent node. Score for the parent node is \langle value\rangle.

\textbf{NE\_REAL\_CHANGED}
\texttt{acc[0]} has changed between calls.
On intermediate entry, \texttt{acc[0]} = \langle value\rangle.
On initial entry, \texttt{acc[0]} = \langle value\rangle.
\texttt{acc[1]} has changed between calls.
On intermediate entry, \texttt{acc[1]} = \langle value\rangle.
On initial entry, \texttt{acc[1]} = \langle value\rangle.
\texttt{gamma} has changed between calls.
On intermediate entry, \texttt{gamma} = \langle value\rangle.
On initial entry, \texttt{gamma} = \langle value\rangle.

\textbf{NE\_TOO\_MANY}
On entry, \texttt{nbest} = \langle value\rangle.
But only \langle value\rangle best subsets could be calculated.

\textbf{NE\_TOO\_SMALL}
On entry, \texttt{licomm} = \langle value\rangle, \texttt{lrcomm} = \langle value\rangle.
Constraint: \texttt{licomm} \geq \langle value\rangle, \texttt{lrcomm} \geq \langle value\rangle.
\texttt{icomm} is too small to return the required array sizes.

7 Accuracy
The subsets returned by \texttt{nag\_best\_subset\_given\_size\_revcomm (h05aac)} are guaranteed to be optimal up to the accuracy of your calculated scores.

8 Parallelism and Performance
\texttt{nag\_best\_subset\_given\_size\_revcomm (h05aac)} is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.
Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users’ Note for your implementation for any additional implementation-specific information.

9 Further Comments

The maximum number of unique subsets of size \( p \) from a set of \( m \) features is \( N = \frac{m^!}{(m-p)!p!} \). The efficiency of the branch and bound algorithm implemented in nag_best_subset_given_size_revcomm (h05aac) comes from evaluating subsets at internal nodes of the tree, that is subsets with more than \( p \) features, and where possible trimming branches of the tree based on the scores at these internal nodes as described in Narendra and Fukunaga (1977). Because of this it is possible, in some circumstances, for more than \( N \) subsets to be evaluated. This will tend to happen when most of the features have a similar effect on the subset score.

If multiple optimal subsets exist with the same score, and \texttt{nbest} is too small to return them all, then the choice of which of these optimal subsets is returned is arbitrary.

10 Example

This example finds the three linear regression models, with five variables, that have the smallest residual sums of squares when fitted to a supplied dataset. The data used in this example was simulated.

10.1 Program Text

```c
/* nag_best_subset_given_size_revcomm (h05aac) Example Program. */
/* Copyright 2014 Numerical Algorithms Group. */
/* Mark 23, 2011. */
/* Pre-processor includes */
#include <stdio.h>
#include <math.h>
#include <string.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagh05.h>
#define BZ(I,J) bz[(J)*(m - ip) + (I)]

typeof struct { 
   Integer n, tdq, tdx;
   double tol;
   Integer *sx;
   Nag_IncludeMean mean;
} calc_subset_data;
void read_subset_data(Integer m, calc_subset_data *cs);
void tidy_subset_data(calc_subset_data *cs);
void calc_subset_score(Integer m,Integer drop,Integer lz,const Integer z[], Integer la,const Integer a[],double bscore[], calc_subset_data *cs);

int main(void)
{
   int exit_status = 0;

   /* Integer scalar and array declarations */
   Integer cnt, drop, i, ip, irevcm, j, la, licomm, lrcomm, lz, m,
   mincnt, mincr, mip, nbest;
   Integer *a = 0, *bz = 0, *ibz = 0, *icomm = 0, *z = 0, *id = 0;
```

/* NAG structures */
NagError fail;

/* Double scalar and array declarations */
double gamma;
double *bscore = 0, *rcomm = 0;
double acc[2];

/* Other data types */
calc_subset_data cs;

/* Initialise the error structure */
INIT_FAIL(fail);

printf("nag_best_subset_given_size_revcomm (h05aac) Example Program Results");
printf("n\n");
#ifdef _WIN32
scanf_s("%*[\n] %*[\n] ");
#else
scanf("%*[\n] %*[\n] ");
#endif

#ifdef _WIN32
scanf_s("%"NAG_IFMT"%"NAG_IFMT"%"NAG_IFMT"%*[\n] ", &m, &ip, &nbest);
#else
scanf("%"NAG_IFMT"%"NAG_IFMT"%"NAG_IFMT"%*[\n] ", &m, &ip, &nbest);
#endif

#ifdef _WIN32
scanf_s("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &mincr, &mincnt, &gamma,
&acc[0], &acc[1]);
#else
scanf("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &mincr, &mincnt, &gamma,
&acc[0], &acc[1]);
#endif

#ifdef _WIN32
scanf_s("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &mincr, &mincnt, &gamma,
&acc[0], &acc[1]);
#else
scanf("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &mincr, &mincnt, &gamma,
&acc[0], &acc[1]);
#endif

/* Read in the problem size */
#ifdef _WIN32
scanf_s("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &m, &ip, &nbest);
#else
scanf("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &m, &ip, &nbest);
#endif

/* Read in the control parameters for the subset selection */
#ifdef _WIN32
scanf_s("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &mincr, &mincnt, &gamma,
&acc[0], &acc[1]);
#else
scanf("%"NAG_IFMT"%"NAG_IFMT"%lf%lf%lf%*[\n] ", &mincr, &mincnt, &gamma,
&acc[0], &acc[1]);
#endif

/* Read in the data required for the score function */
read_subset_data(m, &cs);

/* Allocate memory required by the subset selection routine */
mip = m - ip;
if (!(a = NAG_ALLOC(mip, Integer)) ||
  !(z = NAG_ALLOC(mip, Integer)) ||
  !(bz = NAG_ALLOC(mip*nbest, Integer)) ||
  !(bscore = NAG_ALLOC(MAX(nbest,m),double))) {
  printf("Allocation failure\n");
  exit_status = -1;
  goto END;
}

/* Allocate dummy communication arrays, as we will query the required size */
licomm = 2;
lrcomm = 0;
if (!(icomm = NAG_ALLOC(licomm, Integer)) ||
  !(rcomm = NAG_ALLOC(lrcomm,double))) {
  printf("Allocation failure\n");
  exit_status = -2;
  goto END;
}

/* Query the required length for the communication arrays */
irevcm = 0;
ag_best_subset_given_size_revcomm(&irevcm, mincr, m, ip, nbest, &drop,
  &lz, z, &la, a, bscore, bz, mincnt, gamma,
  acc, icomm, licomm, rcomm, lrcomm, &fail);

/* Extract the required sizes from the communication array */
licomm = icomm[0];
lrcomm = icomm[1];

/* Reallocate communication arrays to the correct size */
NAG_FREE(icomm);
NAG_FREE(rcomm);
if (!((icomm = NAG_ALLOC(licomm, Integer)) ||
    (rcomm = NAG_ALLOC(lrcomm, double))) {
    printf("Allocation failure\n");
    exit_status = -3;
    goto END;
}

/* Initialise reverse communication control flag */
irevcm = 0;

/* Call the reverse communication best subset routine
   (nag_best_subset_given_size_revcomm (h05aac)) in a loop.
   The loop should terminate when irevcm = 0 on exit */
for (cnt = 0;;) {
    nag_best_subset_given_size_revcomm(&irevcm, mincr, m, ip, nbest, &drop,
        &lz, z, &la, a, bscore, bz, mincnt,
        gamma, acc, icomm, licomm, rcomm,
        lrcomm, &fail);
    if (irevcm==0) {
        if (fail.code != NE_NOERROR) {
            printf("Error from nag_best_subset_given_size_revcomm (h05aac).\n%s\n", fail.message);
            if (fail.code != NE_ARG_TOO_LARGE) {
                exit_status = 1;
                goto END;
            }
        }
        /* Jump out of the loop */
        break;
    }

    /* Calculate and return the score for the required models and keep track of
    the number of subsets evaluated */
    cnt += MAX(1,la);
    calc_subset_score(m,drop,lz,z,la,a,bscore,&cs);
}

/* Titles */
printf(" Score Feature Subset\n");
printf(" ----- --------------\n");

/* Display the best subsets and corresponding scores.
 * nag_best_subset_given_size_revcomm returns a list of features excluded
 * from the best subsets, so this is inverted to give the set of features
 * included in each subset.
 * *
 * if (!{id = NAGALLOC(m, Integer)}) {
 *     printf("Allocation failure\n");
 *     exit_status = -1;
 *     goto END;
 * }
 * for (i = 0; i < la; i++) {
 *     printf("%12.5e ", bscore[i]);
 *     for (j = 0; j < m; j++)
 *         id[j] = 1;
 *     for (j = 0; j < mip; j++)
 *         id[BZ(j,i) - 1] = 0;
 *     for (j = 0; j < m; j++)
 *         if (id[j]) printf(" %5"NAG_IFMT, j+1);
 *     printf("\n");
 * }
 * printf("\n");
 * if (fail.code == NE_TOO_MANY) {
 *     printf("%"NAG_IFMT "subsets of the requested size do not exist,"
 *                " only %"NAG_IFMT " are displayed.\n", nbest,la);
 * }

printf("%"NAG_IFMT" subsets evaluated in total\n", cnt);

END:
NAG_FREE(z);
NAG_FREE(a);
NAG_FREE(bz);
NAG_FREE(ibz);
NAG_FREE(bscore);
NAG_FREE(icomm);
NAG_FREE(rcomm);
NAG_FREE(id);
tidy_subset_data(&cs);
return exit_status;
}
#define CSX(I, J) cs->x[(I) * cs->tdx + J]
void read_subset_data(Integer m, calc_subset_data *cs) {
    /* Read in the data, from stdout, and allocate any arrays that are required by the scoring function calc_subset_score */
    Integer i, j;
cs->sx = 0;
cs->x = cs->y = cs->b = cs->se = cs->cov = cs->res = cs->h = cs->q = 0;
cs->p = cs->com_ar = cs->wt = 0;

    /* Skip heading in data file */
    #ifdef _WIN32
        scanf_s("%*[\n] ");
    #else
        scanf("%*[\n] ");
    #endif

    /* Read in the number of observations for the data used in the linear regression */
    #ifdef _WIN32
        scanf_s("%"NAG_IFMT"%*[\n] ", &cs->n);
    #else
        scanf("%"NAG_IFMT"%*[\n] ", &cs->n);
    #endif

    /* Read in the control parameters for the linear regression */
    #ifdef _WIN32
        scanf_s("%lf%*[\n] ", &cs->tol);
    #else
        scanf("%lf%*[\n] ", &cs->tol);
    #endif

    /* Read in the data */
    cs->tdx = m;
    if (!(cs->x = NAG_ALLOC(cs->tdx*cs->n, double)) ||
         !(cs->y = NAG_ALLOC(cs->n, double))) {
        printf("Allocation failure\n");
        tidy_subset_data(cs);
        exit(-1);
    }

    /* Read in the data for the linear regression */
    for (i = 0; i < cs->n; i++) {
        for (j = 0; j < m; j++)
            #ifdef _WIN32
                scanf_s("%lf", &CSX(i,j));
            #else
                scanf("%lf", &CSX(i,j));
            #endif
        #ifdef _WIN32
            scanf_s("%lf%*[\n] ", &cs->y[i]);
        #else
            scanf("%lf%*[\n] ", &cs->y[i]);
        #endif
    }
}

/* h - Operations Research */

Mark 25
/* No intercept term and no weights */
cs->mean = Nag_MeanZero;

/* Allocate memory required by the regression routine */
cs->tdq = cs->n;
if (!(cs->sx = NAG_ALLOC(m, Integer)) ||
    !(cs->b = NAG_ALLOC(m, double)) ||
    !(cs->se = NAG_ALLOC(m, double)) ||
    !(cs->cov = NAG_ALLOC(m*(m+1)/2, double)) ||
    !(cs->res = NAG_ALLOC(cs->n, double)) ||
    !(cs->h = NAG_ALLOC(cs->n, double)) ||
    !(cs->q = NAG_ALLOC(cs->n*cs->tdq, double)) ||
    !(cs->p = NAG_ALLOC(2*m+m*m, double)) ||
    !(cs->com_ar = NAG_ALLOC(5*(m-1)*m*m, double))) {
    printf("Allocation failure\n");
tidy_subset_data(cs);
    exit(-1);
}

void tidy_subset_data(calc_subset_data *cs) {
    /* Tidy up the data structure used by calc_subset_score */
    NAG_FREE(cs->sx);
    NAG_FREE(cs->x);
    NAG_FREE(cs->y);
    NAG_FREE(cs->b);
    NAG_FREE(cs->se);
    NAG_FREE(cs->cov);
    NAG_FREE(cs->res);
    NAG_FREE(cs->h);
    NAG_FREE(cs->q);
    NAG_FREE(cs->p);
    NAG_FREE(cs->com_ar);
    NAG_FREE(cs->wt);
}

void calc_subset_score(Integer m, Integer drop, Integer lz, const Integer z[],
    Integer la, const Integer a[], double bscore[],
    calc_subset_data *cs) {
    /* Calculate the score associated with a particular set of feature subsets.*/
    /* m, drop, lz, z, la, a and bscore are all as described in the documentation*/
    /* of nag_best_subset_given_size_revcomm (h05aac).*/
    /* cs - Structure of type calc_subset_data that holds any additional data*/
    /* required by this routine*/

    This particular example finds the set, of a given size, of explanatory
    variables that best fit a response variable when a linear regression model
    is used. Therefore the feature set is the set of all the explanatory
    variables and the best set of features is defined as set of explanatory
    variables that gives the smallest residual sums of squares. See the
    documentation for g02dac for details on linear regression models.
    */

    /* Integer scalar and array declarations */
    Integer i, j, inv_drop, ip, irank;

    /* NAG structures */
    NagError fail;

    /* Double scalar and array declarations */
    double rss, df;

    /* Other data types */
    Nag_Boolean svd;

    /* Initialise the error structure */
    INIT_FAIL(fail);

    /* Set up the initial feature set.

If drop = 0, this is the Null set (i.e. no features).
If drop = 1 then this is the full set (i.e. all features) /*
for (i = 0; i < m; i++)
cs->sx[i] = drop;

/* Add (if drop = 0) or remove (if drop = 1) the all the features specified
in Z (note: z refers to its features with values 1 to M, therefore you
must subtract 1 when using z as an array reference) .
*/
inv_drop = (drop == 0) ? 1 : 0;
for (i = 0; i < lz; i++)
cs->sx[z[i] - 1] = inv_drop;

/* Loop over all the elements in a, looping at least once */
for (i = 0; i < MAX(la,1); i++) {
  if (la > 0) {
    /* Reset the feature altered at the last iteration */
    cs->sx[a[i-1] - 1] = drop;
  }
  /* Add or drop the I'th feature in A */
  cs->sx[a[i] - 1] = inv_drop;
}

/* Calculate number of parameters in the regression model */
for (ip = j = 0; j < m; j++) ip += (cs->sx[j] == 1);

/* Fit the regression model (g02dac) */
nag_regsn_mult_linear(cs->mean, cs->n, cs->x, cs->tdx, m, cs->sx,
ip, cs->y, cs->wt, &rss, &df, cs->b, cs->se, cs->cov, cs->res, cs->h,
cs->q, cs->tdq, &svd, &rank, cs->p, cs->tol, cs->com_ar, &fail);

/* Return the score (the residual sums of squares) */
bscore[i] = rss;
}

10.2 Program Data

nag_best_subset_given_size_revcomm (h05aac) Example Program Data

Data required by h05aac
14 5 3 :: m,ip,nbest
0 -1 -1.0 -1.0 -1.0 :: mincr, mincnt, gamma, acc[0], acc[1]

Data required by the scoring function
40 :: n
1e-6 :: tol

-1.59 0.19 0.40 0.43 -0.40 0.79 0.06
0.33 1.60 0.58 -1.12 1.23 1.07 -0.07 -2.44
-0.25 0.61 -0.36 1.16 0.61 -2.05 -0.02
-0.04 0.80 -0.73 -0.63 -0.75 -0.73 1.43 -2.97
-2.28 0.46 -0.65 0.33 0.16 -0.21 -1.61
-0.54 0.48 0.37 -0.95 -2.14 0.48 2.02
-0.52 1.05 0.64 0.02 -1.12 0.23 0.06
-1.26 1.40 -0.98 2.47 0.49 -0.02 -0.05 3.00
-0.84 1.86 0.10 0.73 -1.41 0.98 0.20
-0.89 1.84 2.56 0.60 -0.12 0.71 0.23 8.83
1.12 -0.51 -0.58 0.09 -1.14 2.11 -0.11
-0.34 -1.04 -0.43 -0.01 -0.38 1.80 0.05 0.03
0.06 -0.85 -2.09 0.22 -1.35 -0.36 1.20
0.41 0.80 -0.28 0.18 0.27 0.92 0.63 2.57
-0.48 -1.02 0.08 -0.06 0.13 -1.18 2.30
0.03 0.45 0.62 -1.97 0.97 0.93 -0.18 8.31
0.08 -0.31 0.43 -0.38 0.01 1.30 0.66
0.65 -0.59 0.76 0.04 0.17 -0.76 -0.90 4.55
0.66 1.14 0.40 2.37 1.10 0.17 -0.38
1.15 -1.00 -0.13 -0.69 -0.62 -0.18 0.00 -23.10
-1.08 -0.21 -1.13 -0.79 -0.76 -1.58 0.38
<table>
<thead>
<tr>
<th>x</th>
<th>y</th>
<th>x</th>
<th>y</th>
<th>x</th>
<th>y</th>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.26</td>
<td>-0.51</td>
<td>-0.75</td>
<td>0.86</td>
<td>0.29</td>
<td>0.68</td>
<td>3.38</td>
<td></td>
</tr>
<tr>
<td>-1.59</td>
<td>0.58</td>
<td>-1.09</td>
<td>1.18</td>
<td>-1.70</td>
<td>-1.02</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.05</td>
<td>1.30</td>
<td>-0.98</td>
<td>-1.36</td>
<td>-1.28</td>
<td>-1.32</td>
<td>-0.13</td>
<td></td>
</tr>
<tr>
<td>-1.58</td>
<td>-1.30</td>
<td>-0.10</td>
<td>-1.34</td>
<td>0.65</td>
<td>-0.56</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.73</td>
<td>-0.32</td>
<td>2.19</td>
<td>-0.49</td>
<td>0.69</td>
<td>0.18</td>
<td>5.47</td>
<td></td>
</tr>
<tr>
<td>-3.09</td>
<td>-0.61</td>
<td>-1.89</td>
<td>0.15</td>
<td>0.77</td>
<td>-0.49</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.20</td>
<td>-0.04</td>
<td>1.02</td>
<td>0.31</td>
<td>0.81</td>
<td>-0.45</td>
<td>13.97</td>
<td></td>
</tr>
<tr>
<td>1.57</td>
<td>-1.50</td>
<td>-1.45</td>
<td>0.21</td>
<td>0.06</td>
<td>0.24</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-1.34</td>
<td>0.30</td>
<td>1.39</td>
<td>-0.38</td>
<td>-0.71</td>
<td>0.48</td>
<td>20.94</td>
<td></td>
</tr>
<tr>
<td>1.40</td>
<td>-1.40</td>
<td>-0.90</td>
<td>0.36</td>
<td>-0.21</td>
<td>-0.97</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.26</td>
<td>0.08</td>
<td>0.06</td>
<td>-1.49</td>
<td>0.43</td>
<td>-1.61</td>
<td>-12.87</td>
<td></td>
</tr>
<tr>
<td>1.50</td>
<td>-0.61</td>
<td>-0.25</td>
<td>-1.01</td>
<td>-0.43</td>
<td>1.90</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.96</td>
<td>-0.02</td>
<td>0.51</td>
<td>-1.38</td>
<td>-0.78</td>
<td>1.82</td>
<td>28.26</td>
<td></td>
</tr>
<tr>
<td>1.02</td>
<td>3.50</td>
<td>0.10</td>
<td>0.50</td>
<td>0.04</td>
<td>0.61</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-2.69</td>
<td>-0.64</td>
<td>-0.34</td>
<td>-0.21</td>
<td>-1.97</td>
<td>-0.19</td>
<td>6.89</td>
<td></td>
</tr>
<tr>
<td>0.67</td>
<td>-0.38</td>
<td>-0.63</td>
<td>-0.24</td>
<td>1.21</td>
<td>-0.09</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-2.20</td>
<td>1.72</td>
<td>0.29</td>
<td>0.66</td>
<td>0.19</td>
<td>-0.57</td>
<td>5.37</td>
<td></td>
</tr>
<tr>
<td>-0.56</td>
<td>-0.41</td>
<td>1.22</td>
<td>-0.30</td>
<td>0.77</td>
<td>0.82</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.18</td>
<td>1.87</td>
<td>-1.48</td>
<td>0.52</td>
<td>1.35</td>
<td>0.13</td>
<td>-1.50</td>
<td></td>
</tr>
<tr>
<td>-1.10</td>
<td>-0.83</td>
<td>0.71</td>
<td>1.99</td>
<td>-0.24</td>
<td>1.30</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.70</td>
<td>0.28</td>
<td>0.16</td>
<td>0.27</td>
<td>0.37</td>
<td>-1.79</td>
<td>-23.00</td>
<td></td>
</tr>
<tr>
<td>0.60</td>
<td>-0.45</td>
<td>-0.26</td>
<td>-0.23</td>
<td>0.89</td>
<td>0.87</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.20</td>
<td>0.28</td>
<td>0.79</td>
<td>2.76</td>
<td>0.35</td>
<td>1.31</td>
<td>14.09</td>
<td></td>
</tr>
<tr>
<td>0.62</td>
<td>-0.59</td>
<td>1.52</td>
<td>0.62</td>
<td>0.21</td>
<td>1.31</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.36</td>
<td>-0.34</td>
<td>-0.03</td>
<td>-0.59</td>
<td>-1.70</td>
<td>-0.03</td>
<td>-11.05</td>
<td></td>
</tr>
<tr>
<td>-1.45</td>
<td>-0.98</td>
<td>2.10</td>
<td>-1.09</td>
<td>-0.53</td>
<td>-0.38</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.13</td>
<td>0.70</td>
<td>-1.51</td>
<td>0.08</td>
<td>-0.62</td>
<td>-0.64</td>
<td>-32.04</td>
<td></td>
</tr>
<tr>
<td>-0.86</td>
<td>0.70</td>
<td>-1.07</td>
<td>-0.76</td>
<td>0.72</td>
<td>-0.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-1.58</td>
<td>0.00</td>
<td>0.58</td>
<td>-0.21</td>
<td>1.30</td>
<td>2.02</td>
<td>1.52</td>
<td>23.36</td>
</tr>
<tr>
<td>-0.48</td>
<td>0.01</td>
<td>1.30</td>
<td>0.58</td>
<td>-0.54</td>
<td>1.09</td>
<td>0.91</td>
<td></td>
</tr>
<tr>
<td>1.32</td>
<td>-1.20</td>
<td>-0.59</td>
<td>-0.51</td>
<td>0.20</td>
<td>-1.74</td>
<td>-5.58</td>
<td></td>
</tr>
<tr>
<td>-1.41</td>
<td>-0.58</td>
<td>-1.29</td>
<td>1.61</td>
<td>-0.35</td>
<td>-0.72</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-1.09</td>
<td>0.56</td>
<td>-0.87</td>
<td>-0.71</td>
<td>1.25</td>
<td>0.10</td>
<td>2.48</td>
<td></td>
</tr>
<tr>
<td>0.69</td>
<td>1.34</td>
<td>-0.32</td>
<td>2.84</td>
<td>-1.43</td>
<td>-0.47</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.01</td>
<td>-0.72</td>
<td>-0.78</td>
<td>0.50</td>
<td>-1.22</td>
<td>0.54</td>
<td>-5.30</td>
<td></td>
</tr>
<tr>
<td>0.26</td>
<td>0.15</td>
<td>-0.57</td>
<td>0.93</td>
<td>1.33</td>
<td>-0.23</td>
<td></td>
<td></td>
</tr>
<tr>
<td>-0.76</td>
<td>0.25</td>
<td>-1.96</td>
<td>0.39</td>
<td>0.24</td>
<td>-0.26</td>
<td>-7.77</td>
<td></td>
</tr>
<tr>
<td>-0.91</td>
<td>0.23</td>
<td>-0.19</td>
<td>1.58</td>
<td>-0.27</td>
<td>0.33</td>
<td>-0.60</td>
<td></td>
</tr>
<tr>
<td>-0.30</td>
<td>-0.81</td>
<td>-0.95</td>
<td>0.88</td>
<td>-0.09</td>
<td>-0.35</td>
<td>-34.25</td>
<td></td>
</tr>
<tr>
<td>0.65</td>
<td>-1.14</td>
<td>1.18</td>
<td>-1.06</td>
<td>-0.68</td>
<td>-0.22</td>
<td>0.21</td>
<td></td>
</tr>
<tr>
<td>1.08</td>
<td>0.81</td>
<td>-0.33</td>
<td>0.42</td>
<td>-0.90</td>
<td>0.49</td>
<td>26.78</td>
<td></td>
</tr>
<tr>
<td>-0.36</td>
<td>-0.50</td>
<td>-0.02</td>
<td>-0.04</td>
<td>0.77</td>
<td>0.62</td>
<td>-1.35</td>
<td></td>
</tr>
<tr>
<td>1.20</td>
<td>1.22</td>
<td>0.18</td>
<td>-1.39</td>
<td>-0.81</td>
<td>-0.99</td>
<td>-11.85</td>
<td></td>
</tr>
<tr>
<td>-1.16</td>
<td>1.06</td>
<td>0.28</td>
<td>0.14</td>
<td>0.62</td>
<td>-0.80</td>
<td>-1.08</td>
<td></td>
</tr>
<tr>
<td>1.37</td>
<td>1.57</td>
<td>-1.48</td>
<td>-0.79</td>
<td>0.28</td>
<td>-0.20</td>
<td>-8.62</td>
<td></td>
</tr>
<tr>
<td>0.50</td>
<td>0.13</td>
<td>-0.68</td>
<td>0.26</td>
<td>-1.13</td>
<td>0.62</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.39</td>
<td>1.14</td>
<td>0.15</td>
<td>1.03</td>
<td>0.46</td>
<td>0.40</td>
<td>12.35</td>
<td></td>
</tr>
<tr>
<td>-0.61</td>
<td>0.93</td>
<td>-0.37</td>
<td>0.44</td>
<td>-1.45</td>
<td>0.58</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.72</td>
<td>-2.05</td>
<td>-0.03</td>
<td>-1.24</td>
<td>-1.40</td>
<td>-0.06</td>
<td>-1.54</td>
<td></td>
</tr>
<tr>
<td>0.67</td>
<td>0.04</td>
<td>0.27</td>
<td>-0.84</td>
<td>-0.06</td>
<td>-3.67</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.66</td>
<td>-0.30</td>
<td>1.67</td>
<td>1.08</td>
<td>0.00</td>
<td>0.43</td>
<td>-16.59</td>
<td></td>
</tr>
<tr>
<td>1.06</td>
<td>0.28</td>
<td>0.14</td>
<td>0.62</td>
<td>-0.80</td>
<td>-1.08</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.08</td>
<td>0.94</td>
<td>0.49</td>
<td>-0.56</td>
<td>0.95</td>
<td>1.09</td>
<td>-8.69</td>
<td></td>
</tr>
<tr>
<td>-0.02</td>
<td>1.18</td>
<td>-1.16</td>
<td>0.49</td>
<td>1.56</td>
<td>-0.60</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.72</td>
<td>-1.20</td>
<td>2.52</td>
<td>1.78</td>
<td>0.16</td>
<td>-0.01</td>
<td>7.82</td>
<td></td>
</tr>
<tr>
<td>0.73</td>
<td>-1.23</td>
<td>1.50</td>
<td>0.40</td>
<td>-0.20</td>
<td>-0.65</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.09</td>
<td>0.40</td>
<td>-1.50</td>
<td>-2.10</td>
<td>0.21</td>
<td>-0.18</td>
<td>-18.56</td>
<td></td>
</tr>
<tr>
<td>-0.01</td>
<td>0.85</td>
<td>-2.04</td>
<td>1.17</td>
<td>-0.56</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
| 1.18 | -0.96 | -0.92 | -0.28 | 1.58 | 17.21 :: x,y
10.3 Program Results

nag_best_subset_given_size_revcomm (h05aac) Example Program Results

<table>
<thead>
<tr>
<th>Score</th>
<th>Feature Subset</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.04753e+03</td>
<td>4 7 8 10 14</td>
</tr>
<tr>
<td>1.05987e+03</td>
<td>4 5 7 8 14</td>
</tr>
<tr>
<td>1.07016e+03</td>
<td>4 5 7 10 14</td>
</tr>
</tbody>
</table>

45 subsets evaluated in total