NAG Library Function Document

nag_daxpby (f16ecc)

1 Purpose
nag_daxpby (f16ecc) computes the sum of two scaled vectors, for real vectors and scalars.
nag_daxpby (f16ecc) performs the operation

\[ y \leftarrow \alpha x + \beta y . \]

2 Specification
#include <nag.h>
#include <nagf16.h>
void nag_daxpby (Integer n, double alpha, const double x[], Integer incx,
                 double beta, double y[], Integer incy, NagError *fail)

3 Description
nag_daxpby (f16ecc) performs the operation

\[ y \leftarrow \alpha x + \beta y \]

where \( x \) and \( y \) are \( n \)-element real vectors, and \( \alpha \) and \( \beta \) real scalars. If \( n \) is equal to zero, or if \( \alpha \) is equal to zero and \( \beta \) is equal to 1, this function returns immediately.

4 References

5 Arguments
1: \( n \) – Integer \hspace{1cm} \text{Input}
   \text{On entry:} \ n, \text{ the number of elements in } x \text{ and } y. 
   \text{Constraint:} \ n \geq 0.

2: \( \alpha \) – double \hspace{1cm} \text{Input}
   \text{On entry:} \ \text{the scalar } \alpha. 

3: \( x[\text{dim}] \) – const double \hspace{1cm} \text{Input}
   \text{On entry:} \ \text{the } n\text{-element vector } x. 
   \text{If } \text{incx} > 0, \ x_i \text{ must be stored in } x[(i - 1) \times |\text{incx}|], \text{ for } i = 1, 2, \ldots, n. 
   \text{If } \text{incx} < 0, \ x_i \text{ must be stored in } x[(n - i) \times |\text{incx}| - 2], \text{ for } i = 1, 2, \ldots, n. 
   \text{Intermediate elements of } x \text{ are not referenced.}
4: \texttt{incx} – Integer \hspace{1cm} \textit{Input}

\textit{On entry}: the increment in the subscripts of \(x\) between successive elements of \(x\).
\textit{Constraint}: \(\texttt{incx} \neq 0\).

5: \texttt{beta} – double \hspace{1cm} \textit{Input}

\textit{On entry}: the scalar \(\beta\).

6: \texttt{y[dim]} – double \hspace{1cm} \textit{Input/Output}

\textit{Note}: the dimension, \(dim\), of the array \(y\) must be at least \(\max(1, 1 + (n - 1) \times |\texttt{incy}|)\).

\textit{On entry}: the \(n\)-element vector \(y\).
If \(\texttt{incy} > 0\), \(y\) must be stored in \(y[1 + (i - 1) \times \texttt{incy}]\), for \(i = 1, 2, \ldots, n\).
If \(\texttt{incy} < 0\), \(y\) must be stored in \(y[1 - (n - i) \times \texttt{incy}]\), for \(i = 1, 2, \ldots, n\).
Intermediate elements of \(y\) are not referenced.
\textit{On exit}: the updated vector \(y\) stored in the array elements used to supply the original vector \(y\).
Intermediate elements of \(y\) are unchanged.

7: \texttt{incy} – Integer \hspace{1cm} \textit{Input}

\textit{On entry}: the increment in the subscripts of \(y\) between successive elements of \(y\).
\textit{Constraint}: \(\texttt{incy} \neq 0\).

8: \texttt{fail} – NagError * \hspace{1cm} \textit{Input/Output}

The NAG error argument (see Section 3.6 in the Essential Introduction).

6 \hspace{1cm} \textbf{Error Indicators and Warnings}

\textbf{NE_ALLOC_FAIL} 
Dynamic memory allocation failed.
See Section 3.2.1.2 in the Essential Introduction for further information.

\textbf{NE_BAD_PARAM} 
On entry, argument \(\langle\text{value}\rangle\) had an illegal value.

\textbf{NE_INT} 
On entry, \texttt{incx} = \(\langle\text{value}\rangle\).
Constraint: \texttt{incx} \(\neq 0\).
On entry, \texttt{incy} = \(\langle\text{value}\rangle\).
Constraint: \texttt{incy} \(\neq 0\).
On entry, \(n = \langle\text{value}\rangle\).
Constraint: \(n \geq 0\).

\textbf{NE_INTERNAL_ERROR} 
An unexpected error has been triggered by this function. Please contact NAG.
See Section 3.6.6 in the Essential Introduction for further information.

\textbf{NE_NO_LICENCE} 
Your licence key may have expired or may not have been installed correctly.
See Section 3.6.5 in the Essential Introduction for further information.
7 Accuracy

The BLAS standard requires accurate implementations which avoid unnecessary over/underflow (see Section 2.7 of Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001)).

8 Parallelism and Performance

nag_daxpby (f16ecc) is not threaded by NAG in any implementation.

nag_daxpby (f16ecc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the X06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users’ Note for your implementation for any additional implementation-specific information.

9 Further Comments

None.

10 Example

This example computes the result of a scaled vector accumulation for

\[
\begin{align*}
\alpha &= 3, & x &= (-4,2.1,3.7,4.5,-6)\top, \\
\beta &= -1, & y &= (-3,-2.4,6.4,-5,-5.1)\top.
\end{align*}
\]

See Section 10 in nag_real_banded_sparse_eigensystem_sol (f12agc) and nag_real_symm_banded_sparse_eigensystem_sol (f12fgc).

10.1 Program Text

/* nag_daxpby (f16ecc) Example Program. */
/* Copyright 2014 Numerical Algorithms Group. */
/* Mark 24, 2013. */
*/
#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf16.h>
int main(void)
{
    /* Scalars */
    Integer exit_status, i, incx, incy, n, xlen, ylen;
    double alpha, beta;
    /* Arrays */
    double *x = 0, *y = 0;
    /* Nag Types */
    NagError fail;
    exit_status = 0;
    INIT_FAIL(fail);
    printf("nag_daxpby (f16ecc) Example Program Results\n\n");
    /* Skip heading in data file */
    #ifdef _WIN32
    scanf_s("%*[\n ]");
    #else
    scanf("%*[\n ]");
    #endif

/* Read number of elements */
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%*[\n] ", &n);
#else
    scanf("%"NAG_IFMT"%*[\n] ", &n);
#endif
/* Read increments */
#ifdef _WIN32
    scanf_s("%"NAG_IFMT"%"NAG_IFMT"%*[\n] ", &incx, &incy);
#else
    scanf("%"NAG_IFMT"%"NAG_IFMT"%*[\n] ", &incx, &incy);
#endif
/* Read factors alpha and beta */
#ifdef _WIN32
    scanf_s("%lf%lf%*[\n] ", &alpha, &beta);
#else
    scanf("%lf%lf%*[\n] ", &alpha, &beta);
#endif
xlen = MAX(1, 1 + (n - 1)*ABS(incx));
ylen = MAX(1, 1 + (n - 1)*ABS(incy));
if (n > 0)
{
    /* Allocate memory */
    if (!(x = NAG_ALLOC(xlen, double)) ||
        !(y = NAG_ALLOC(ylen, double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    else
    {
        printf("Invalid n\n");
        exit_status = 1;
        goto END;
    }
}
/* Input vector x */
#ifdef _WIN32
    scanf_s("%lf", &x[i]);
#else
    scanf("%lf", &x[i]);
#endif
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif
/* Input vector y */
#ifdef _WIN32
    scanf_s("%lf", &y[i]);
#else
    scanf("%lf", &y[i]);
#endif
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

/* nag_daxpby (f16ecc). * Performs y := alpha*x + beta*y */
if (fail.code != NE_NOERROR)
printf("Error from nag_daxpby (f16ecc).\n%s\n", fail.message);
exit_status = 1;
goto END;
}

/* Print the result */
printf("Result of the scaled vector accumulation is\n");
printf("y = (\n");
for (i = 0; i < ylen - 1; i = i + abs(incy))
    printf("%9.4f, ", y[i]);
printf("%9.4f)\n", y[ylen - 1]);

END:
NAG_FREE(x);
NAG_FREE(y);
return exit_status;
}

10.2 Program Data
nag_daxpby (f16ecc) Example Program Data

<table>
<thead>
<tr>
<th>n</th>
<th>incx and incy</th>
<th>alpha and beta</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>-1 -1</td>
<td>3.0 -1.0</td>
<td>-4.0  2.1 3.7 4.5 -6.0</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>-3.0  -2.4 6.4 -5.0 -5.1</td>
</tr>
</tbody>
</table>

10.3 Program Results
nag_daxpby (f16ecc) Example Program Results

Result of the scaled vector accumulation is
y = ( -9.0000,  8.7000,  4.7000, 18.5000, -12.9000)